## A FEWTHINGS ABOUT

# DEEP LEARNING 

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November 2013

## WIRED

"The Man Behind the Google Brain: Andrew Ng and the Quest for the New Al'"
www.wired.com/wiredenterprise/
20|3/05/neuro-artificial-intelligence/all/

# WIRED 

"The Man Behind the Google Brain: Andrew Vg and the Quest for the New Al'"

## © fo Attu lock Times

## How Many Computers

to Identify a Cat?
16,000
www.nytimes.com/20|2/06/26/
technology/in-a-big-network-of-
computers-evidence-of-machine-
learning.html

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"The Man Behind the Google Brain: Andrew Ng and the Quest for the New Al"
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## The Anu lock Times

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technology/in-a-big-network-of-computers-evidence-of-machinelearning.html

## MIT Technology Review

With massive amounts of computational power, machines can now recognize objects and translate speech in real time. Artificial intelligence is finally getting smart.
www.technologyreview.com/ featuredstory/5 I 3696/deep-learning/

## BREAKTHROUGH RESULTS

# BREAKTHROUGH RESULTS 



Images from
CIFAR-I 0 dataset:
WWW.Cs.toronto.e du/~kriz/cifar.html

## BREAKTHROUGH RESULTS

## Object Recognition



Why is<br>it so<br>hard?

Images from
CIFAR-I 0 dataset:
www.cs.toronto.e du/~kriz/cifar.html

Object Recognition
IM․․GENET ILSVRC20I2

| Team name | Error (5 guesses) | Description |
| :--- | :--- | :--- |
| SuperVision | 0.15315 | Using extra training data from <br> ImageNet Fall 2011 release |
| SuperVision | 0.16422 | Using only supplied training data |
|  |  | Weighted sum of scores from <br> each classifier with SIFT+FV, <br> LBP+FV, GIST+FV, and <br> CSIFT+FV, respectively. |
| ISI | 0.26172 |  |

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## BREAKTHROUGH RESULTS

## Object Recognition



# BREAKTHROUGH RESULTS 

Traffic Sign Recognition

www.idsia.ch/~juergen/ijcnn20 I I.pdf

# BREAKTHROUGH RESULTS 

## Traffic Sign Recognition


www.idsia.ch/~juergen/ijcnn20 I I.pdf

| Rank | Team | Method | Correct recognition rate |
| ---: | :--- | :--- | :--- |
| 1 | IDSIA | Committee of CNNs | $99.46 \%$ |
| 2 | INI | Human Performance | $98.84 \%$ |
| 3 | sermanet | Multi-Scale CNNs | $98.31 \%$ |
| 4 | CAOR | Random Forests | $96.14 \%$ |

# BREAKTHROUGH RESULTS 

Merck Competition<br>Deep NN and GPUs come out to play<br>blog.kaggle.com/20|2/I0/3I/merck-competition-results-deep-nn-and-gpus-come-out-to-play/

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## Microsoft Research Speech Recognition Leaps Forward

research.microsoft.com/en-us/news/features/speechrecognition-0829 | I.aspx

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# Microsoft Research Speech Recognition Leaps Forward 

research.microsoft.com/en-us/news/features/speechrecognition-0829 | I.aspx
and more...

## LARGE ADOPTION

## YAHOO!

## facebook

Microsoft
just to mention a few big names
"artificial intelligence is finally getting smart"
WWw.technologyreview.com/featuredstory/5 | 3696/deep-learning/
"artificial intelligence is finally getting smart"'
Www.technologyreview.com/featuredstory/5 | 3696/deep-learning/

## DON'T TAKE IT THE WRONG WAY

"artificial intelligence is finally getting smart"'
www.technologyreview.com/featuredstory/5 I 3696/deep-learning/

## DON'T TAKE IT THE WRONG WAY

"Biology is hiding secrets well. We just don't have the right tools to grasp the complexity of what's going on."

Bruno Olshausen

## DON’T TAKE IT THE WRONG WAY

"Biology is hiding secrets well. We just don't have the right tools to grasp the complexity of what's going on." Bruno Olshausen
"We clearly don't have the right algorithms yet. It's going to take decades. This is not going to be an easy one, but I think there's hope."
Andrew Ng

# ILSVRC20I2 WINNER 

## Object Recognition

## IM여GENET

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## ILSVRC20I2 WINNER

"Our model is a large, deep convolutional neural network trained on raw RGB pixel values. The neural network, which has 60 million parameters and 650,000 neurons, consists of five convolutional layers, some of which are followed by max-pooling layers, and three globally-connected layers with a final 1000-way softmax. It was trained on two NVIDIA GPUs for about a week.
To make training faster, we used non-saturating neurons and a very efficient GPU implementation of convolutional nets. To reduce overfitting in the globally-connected layers we employed hidden-unit "dropout", a recently-developed regularization method that proved to be very effective."

## WHAT'S NEW?

convolutional neural networks max-pooling layers 60 million parameters non-saturating neurons efficient GPU implementation "dropout"

## WHAT'S NEW?

convolutional neural networks Lecun et al., 1989 max-pooling layers Fukushima, 1980 60 million parameters non-saturating neurons efficient GPU implementation "dropout"

## NEURAL NETWORK RENAISSANCE

## IN 2006

## Hinton et al. showed that

a particular form of autoencoder can be trained and stacked in a greedily manner, so that a bound on the probability of representing well the training data is increased at each layer.

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a particular form of autoencoder can be trained and stacked in a greedily manner, so that a bound on the probability of representing well the training data is increased at each layer.
others paper followed soon after

## IN 2006

## autoencoder

a partic is a neural network stacked probab whose aim is to learn a compressed representation of the input data $\quad$ ng data is (unsupervised)
others paper followed soon after

## KEY PRINCIPLES

unsupervised training of one layer at a time

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unsupervised training of one layer at a time
supervised training of all layers


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unsupervised training of one layer at a time
supervised training of all layers


## KEY PRINCIPLES

unsupervised training of one layer at a time pre-training

supervised training of all layers


## KEY PRINCIPLES

unsupervised training of one layer at a time pre-training
supervised training of all layers fine-tuning


## UNSUPERVISED PRE-TRAINING

a.k.a. unsupervised feature learning

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## idea

learn one
layer of representation at a time on top of the previous one

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learn one<br>nonlinear<br>layer of representation<br>at a time<br>on top of the previous one

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## idea

learn one<br>nonlinear<br>layer of representation at a time on top of the previous one

learn one layer $=$ learn neuron weights to extract one layer

## UNSUPERVISED PRE-TRAINING

a.k.a. unsupervised feature learning

## before that (2006)

deep supervised
feedforward neural networks tended to yield worse results then shallow ones

## UNSUPERVISED PRE-TRAINING

a.k.a. unsupervised feature learning

hypothesis

## UNSUPERVISED PRE-TRAINING

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## hypothesis

learn high-level abstractions of the input

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## hypothesis

learn high-level abstractions of the input
helps fine-tuning to reach a better local minimum

## UNSUPERVISED PRE-TRAINING

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## hypothesis

learn high-level abstractions of the input
helps fine-tuning to reach a better local minimum

better generalization

## UNSUPERVISED PRE-TRAINING

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## motivation

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in many problems, high-level abstractions are impossible to model with human ingenuity

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a.k.a. unsupervised feature learning

## motivation

in many problems, high-level abstractions are impossible to model with human ingenuity
necessity to capture the explanatory factors (structure) of the data

## WHY UNSUPERVISED?

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supervised representation learning in early layers tend to
discard information important for higher concepts

Bengio et al, 2007

## WHY UNSUPERVISED?

supervised representation learning in early layers tend to discard information important for higher concepts

Bengio et al, 2007
it is more biologically plausible:
brain needs to learn $10^{14}$ synapses in $10^{9}$ seconds

## THE IMPORTANCE OF DEPTH

in many cases, depth 2 is enough to represent any function with a given target accuracy

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in many cases, depth 2 is enough to represent any function with a given target accuracy

but the required number of nodes in the graph may grow very large

## THE IMPORTANCE OF DEPTH

functions representable compactly with $k$ layers may require exponential size with $k$ - 1 layers

Hastad et al 86, Hastad et al 91, Bengio et al 2007

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functions representable compactly with $k$ layers may require exponential size with $k$ - 1 layers


Hastad et al 86, Hastad et al 91, Bengio et al 2007


## INTUITION ON DEPTH


sub1
main
subsubsub1
subsubsub2


## INTUITION ON DEPTH


"shallow" computer programs

## THE IMPORTANCE OF DEPTH

## brain has a deep architecture



## THE IMPORTANCE OF DEPTH

## composing concepts | disentangling information



## THE IMPORTANCE OF DEPTH

composing concepts | disentangling information


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## composing concepts | disentangling information



## AFTER ALL

## WHAT'S DEEP LEARNING?

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## HOW DEEP?

## AFTER ALL

## WHAT'S DEEP LEARNING?

"When there is more than one hidden layer being learned, this is deep learning.' Geoffrey Hinton, coursera class

## HOW DEEP?

"When the number of levels can be data selected, this is a deep architecture."

Yoshua Bengio, sstic 2013

## NEURAL NETWORKS RENAISSANCE

In 2006...

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In 2006...
autoencoders

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In 2006...
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pre-training

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AUTOENCODER NEURAL NETS

## AUTOENCODER NEURAL NETS

Is an unsupervised learning algorithm that applies backpropagation, setting the target values to be equal to the inputs.

$$
\hat{f}_{\theta}(x) \approx(x)
$$

## AUTOENCODER NEURAL NETS



## AUTOENCODER NEURAL NETS

tries to learn an approximation to the identity function

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tries to learn an approximation to the identity function
the network is usually forced to learn a compressed representation of the input

## AUTOENCODER NEURAL NETS

tries to learn an approximation to the identity function
the network is usually forced to learn a compressed representation of the input
tries to discover structure in the data

## AUTOENCODER NEURAL NETS

following the notation of previous lectures, we can back propagate the reconstruction error by setting

$$
\begin{aligned}
& \delta_{j}^{(3)}=-\left(x_{j}-a_{j}^{(3)}\right) \cdot * g^{\prime}\left(z^{(3)}\right) \\
& \delta^{(2)}=\left(\left(\theta^{(2)}\right)^{T} \delta^{(3)}\right) \cdot * g^{\prime}\left(z^{(2)}\right)
\end{aligned}
$$

## AUTOENCODER NEURAL NETS

interesting structures can be discovered by placing constraints on the network such as sparsity

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Layer $\mathrm{L}_{1}$

## AUTOENCODER NEURAL NETS

interesting structures can be discovered by placing constraints on the network such as sparsity

$$
\hat{\rho}=\frac{1}{m} \sum_{i=1}^{m}\left[a_{j}^{(2)}\left(x^{(i)}\right)\right]
$$

be the average activation of the hidden unit j (averaged over the training set)

## AUTOENCODER NEURAL NETS

we would like to (approximately) enforce

$$
\hat{\rho}=\rho
$$

## AUTOENCODER NEURAL NETS

we would like to (approximately) enforce

$$
\hat{\rho}=\rho
$$

a possible choice of of penalty to add in the optimization objective is

$$
\sum_{j=1}^{s_{2}} \rho \log \frac{\rho}{\hat{\rho}_{j}}+(1-\rho) \log \frac{1-\rho}{1-\hat{\rho}_{j}}=\sum_{j=1}^{s_{2}} \mathrm{KL}\left(\rho \| \hat{\rho}_{j}\right)
$$

## AUTOENCODER NEURAL NETS



## AUTOENCODER NEURAL NETS

the objective function then becomes

$$
J_{\text {sparse }}(\theta)=J(\theta)+\beta \sum_{j=1}^{s_{2}} \mathrm{KL}\left(\rho \| \hat{\rho}_{j}\right)
$$

## AUTOENCODER NEURAL NETS

the objective function then becomes

$$
J_{\text {sparse }}(\theta)=J(\theta)+\beta \sum_{j=1}^{s_{2}} \mathrm{KL}\left(\rho \| \hat{\rho}_{j}\right)
$$

and

$$
\delta_{i}^{(2)}=\left(\left(\theta_{i}^{(2)}\right)^{T} \delta_{i}^{(3)}\right) \cdot * g^{\prime}\left(z_{i}^{(2)}\right)+\beta\left(-\frac{\rho}{\hat{\rho}_{i}}+\frac{1-\rho}{1-\hat{\rho}_{i}}\right)
$$

## AUTOENCODER NEURAL NETS

visualizing the function learned from image patches

## AUTOENCODER NEURAL NETS

visualizing the function learned from image patches

deeplearning.stanford.edu/wiki/index.php/Autoencoders_and_Sparsity

## STACKED AUTOENCODERS

a NN consisting of multiple layers of autoencoders


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## UNSUPERVISED PRE-TRANING

## BEFORE

 deep architectures performed poorly
## UNSUPERVISED PRE-TRANING

BEFORE deep architectures performed poorly

AFTER<br>state-of-the-art results

BUT...

ILSVRC2012 WINNER
convolutional neural networks Lecun et al., 1989 max-pooling layers Fukushima, 1980 60 million parameters non-saturating neurons efficient GPU implementation "dropout"

## ILSVRC2012 WINNER

convolutional neural networks Lecun et al., 1989 max-pooling layers Fukushima, 1980 60 million parameters non-saturating neurons efficient GPU implementation "dropout"

NO PRE-TRAINING AT ALL!

## ILSVRC2012 WINNER

convolutional neural net layers Fukushima, 1980 max-pooling meters 60 million paramerons non-saturating neurons efficient GPU imp "dropout"

## NO PRE-TRAINING AT ALL!

## CONVOLUTIONAL NEURAL NETWORKS

## FULLY-CONNECTED NNS



## CONVOLUTIONAL NNS

inspired by Hubel and Wiesel cells

# CONVOLUTIONAL NNS 

inspired by Hubel and Wiesel cells

## simple

complex

# CONVOLUTIONAL NNS 

inspired by Hubel and Wiesel cells

## simple

responds maximally to specific local stimulus
complex

## CONVOLUTIONAL NNS

inspired by Hubel and Wiesel cells

## simple

responds maximally to specific local stimulus
complex
local invariance to the exact position of stimulus

## CONVOLUTIONAL NNS

shared (tied) weights


# CONVOLUTIONAL NNS 

shared (tied) weights
layer m-I

hidden layer $m$


# CONVOLUTIONAL NNS 

## shared (tied) weights

$$
\frac{\partial}{\partial \theta_{i j}} J(\theta)=\sum_{p \in \mathcal{P}}\left[a_{j(p)}^{(l)} \delta_{i}^{(l+1)}\right]
$$

$\mathcal{P}$ is the set of all positions where $\theta_{i}$ is convolved

## shared (tied) weights

| $1_{x}$ | $1_{x 0}$ | $1_{x}$ | 0 | 0 |  |
| :--- | :--- | :--- | :--- | :--- | :---: |
| $0_{x 0}$ | $1_{x}$ | $1_{x}$ | 1 | 0 |  |
| $0_{x}$ | $O_{x 0}$ | $1_{x}$ | 1 | 1 |  |
| 0 | 0 | 1 | 1 | 0 |  |
| 0 | 1 | 1 | 0 | 0 |  |
| Image |  |  |  |  |  |
|  |  |  |  |  |  |


| 4 |  |  |
| :--- | :--- | :--- |
|  |  |  |
|  |  |  |

Convolved
Feature

ILSVRC2012 WINNER
convolutional neural networks Lecun et al., 1989 max-pooling layers Fukushima, 1980 60 million parameters non-saturating neurons efficient GPU implementation "dropout"

ILSVRC2012 WINNER
convolutional neural networks Lecun et al., 1989 max-pooling layers Fukushima, 1980 60 million parameters non-saturating neurons efficient GPU implementation "dropout"

## CONVOLUTIONAL NNS

max (or average) pooling units

$$
g\left(a_{j}\right)=\max \left(a_{j,(p)}\right) \quad \forall p \in \mathcal{N}
$$


where $\mathcal{N}$ defines the pooling regions that may or may not overlapped

## CONVOLUTIONAL NNS

max (or average) pooling units

$$
g\left(a_{j}\right)=\max \left(a_{j,(p)}\right) \quad \forall p \in \mathcal{N}
$$


receptive
where $\mathcal{N}$ defines the pooling regions field that may or may not overlapped
max (or average) pooling units


## Convolved feature

Pooled
feature

# CONVOLUTIONAL NETS 

## convolution + pooling



ILSVRC2012 WINNER
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# CONVOLUTIONAL NNS 

non-saturating nonlinearity
rectified linear units

$$
g\left(z^{(l)}\right)=\max \left(0, z^{(l)}\right)
$$

# CONVOLUTIONAL NNS 

non-saturating nonlinearity
rectified linear units

$$
g\left(z^{(l)}\right)=\max \left(0, z^{(l)}\right)
$$

instead of

$$
g\left(z^{(l)}\right)=\frac{1}{1+e^{-z^{(l)}}}
$$

ILSVRC2012 WINNER
convolutional neural networks Lecun et al., 1989 max-pooling layers Fukushima, 1980 60 million parameters non-saturating neurons efficient GPU implementation "dropout"

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## THE 60 MILLION PARAMETER ARCHITECTURE



ILSVRC2012 WINNER
convolutional neural networks Lecun et al., 1989 max-pooling layers Fukushima, 1980 60 million parameters non-saturating neurons efficient GPU implementation "dropout"

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# CONVOLUTIONAL NNS 

## dropout regularization recipe

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set to zero the output of each hidden neuron with probability 0.5

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set to zero the output of each hidden neuron with probability 0.5
neurons "dropped out" contribute neither in the forward pass nor in back-propagation

## CONVOLUTIONAL NNS

## dropout regularization recipe

set to zero the output of each hidden neuron with probability 0.5

neurons "dropped out" contribute neither in the forward pass nor in back-propagation

at test time, use all the neurons
but multiply their outputs by 0.5

# CONVOLUTIONAL NNS 

dropout regularization implications

# CONVOLUTIONAL NNS 

dropout regularization implications
every time an input is presented, the neural network samples a different architecture

# CONVOLUTIONAL NNS 

dropout regularization implications
every time an input is presented, the neural network samples a different architecture
all the sampled architectures share weights

# CONVOLUTIONAL NNS 

dropout regularization implications
every time an input is presented, the neural network samples a different architecture
all the sampled architectures share weights
reduces complex co-adaptations of neurons

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NO PRE-TRAINING AT ALL!

## NO-PRETRAINING AT ALL?

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"if you initialize the layers correctly, you may not need pre-training at all, provided you have enough labeled data"

## NO-PRETRAINING AT ALL?

"if you initialize the layers correctly, you may not need pre-training at all, provided you have enough labeled data"
"however, you can always increase the size of your neural net so that even a huge amount of data is still not enough"

Geoffrey Hinton, Coursera class

## ONTHE ARCHITECTURE



## ONTHE ARCHITECTURE


typically hand-tuned

## ONTHE ARCHITECTURE



## typically hand-tuned

critical in the method's performance

## ONTHE ARCHITECTURE



## typically hand-tuned

critical in the method's performance

## complicated search space

## ONTHE ARCHITECTURE <br> (a) <br> 

(c)

## Candidate Model Scores



## ON THE ARCHITECTURE



## QUICK LAB

using an alternative notation

## CONVOLUTION+ACTIVATION

the filtering operation of an input $\mathbf{n}$ with a bank of $k$ filters is

$$
\mathbf{f}_{i}=\mathbf{n} \otimes \Phi_{i} \quad \forall i \in\{1,2, \ldots, k\}
$$

where $\otimes$ is a 3 D convolution sliding over the first two dimensions, and $\Phi_{i} \in \mathbb{R}^{f h \times f w \times f d}$ is one such filter of our filter bank
and the rectified linear activation is

$$
\mathbf{a}_{i}=\max \left(0, \mathbf{f}_{i}\right)
$$

## POOLING

the pooling operation with strength $p$ and spatial downsampling of $\alpha$ is

$$
\mathbf{p}_{i}=\operatorname{downsample}_{\alpha}\left(\sqrt[p]{\left(\mathbf{a}_{i}\right)^{p} \odot \mathbf{1}_{p h \times p w}}\right),
$$

where $\odot$ is a 2D convolution sliding over both dimensions and $p h \times p w$ is the pooling neighborhood

## DIVISIVE NORMALIZATION

## DIVISIVE NORMALIZATION

"In biology, initial interests in DN focused on its ability to model dynamic gain control in retina [24] and the "masking" behavior in perception [11, 33], and to fit neural recordings from the mammalian visual cortex [12, 19]."

## DIVISIVE NORMALIZATION

finally, the divisive normalization of an input $\mathbf{x} \in \mathbb{R}^{x h \times x w \times x d}$ is

$$
\mathbf{n}=\frac{\mathbf{x}}{\sqrt{\mathbf{x}^{2} \otimes \mathbf{1}_{n h \times n w \times n d}}}
$$

where $\mathbf{1}_{n h \times n w \times x d}$ is a matrix of ones representing the normalization neighborhood
let's get our hands dirty!


## FACE IDENTIFICATION


questions?

