



$$x = \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} \begin{bmatrix} w_{11} & w_{12} \\ w_{21} & w_{22} \end{bmatrix} \begin{bmatrix} b_1 \\ b_2 \end{bmatrix} \begin{bmatrix} w_1 \\ w_2 \end{bmatrix} \begin{bmatrix} b \end{bmatrix}$$

$$\text{MSE} = \frac{1}{4} \sum_x (f(x) - f^*(x))^2$$

$$f(x) = w_1 \sigma(w_{11}x_1 + w_{12}x_2 + b_1) + w_2 \sigma(w_{21}x_1 + w_{22}x_2 + b_2) + b$$

$$\text{MSE} = \frac{1}{4} \sum_x (w_1 \sigma(w_{11}x_1 + w_{12}x_2 + b_1) + w_2 \sigma(w_{21}x_1 + w_{22}x_2 + b_2) + b - f^*(x))^2$$

$$\frac{\partial \text{MSE}}{\partial w_{11}} = \frac{1}{4} \sum_x 2(f(x) - f^*(x)) w_1 \sigma'(w_{11}x_1 + w_{12}x_2 + b_1) x_1$$

$$\frac{\partial \text{MSE}}{\partial w_{12}} = \frac{1}{4} \sum_x 2(f(x) - f^*(x)) w_1 \sigma'(w_{11}x_1 + w_{12}x_2 + b_1) x_2$$

$$\frac{\partial \text{MSE}}{\partial b_1} = \frac{1}{4} \sum_x 2(f(x) - f^*(x)) w_1 \sigma'(w_{11}x_1 + w_{12}x_2 + b_1)$$

$$\frac{\partial \text{MSE}}{\partial w_{21}} = \frac{1}{4} \sum_x 2(f(x) - f^*(x)) w_2 \sigma'(w_{21}x_1 + w_{22}x_2 + b_2) x_1$$

$$\frac{\partial \text{MSE}}{\partial w_{22}} = \frac{1}{4} \sum_x 2(f(x) - f^*(x)) w_2 \sigma'(w_{21}x_1 + w_{22}x_2 + b_2) x_2$$

$$\frac{\partial \text{MSE}}{\partial b_2} = \frac{1}{4} \sum_x 2(f(x) - f^*(x)) w_2 \sigma'(w_{21}x_1 + w_{22}x_2 + b_2)$$

$$\frac{\partial \text{MSE}}{\partial w_1} = \frac{1}{4} \sum_x 2(f(x) - f^*(x)) \sigma(w_{11}x_1 + w_{12}x_2 + b_1)$$

$$\frac{\partial \text{MSE}}{\partial w_2} = \frac{1}{4} \sum_x 2(f(x) - f^*(x)) \sigma(w_{21}x_1 + w_{22}x_2 + b_2)$$

$$\frac{\partial \text{MSE}}{\partial b} = \frac{1}{4} \sum_x 2(f(x) - f^*(x))$$